Understanding of Sets and Venn-Diagrams

HOCHSCHULE FÜR TECHNIK UND WIRTSCHAFT DRESDEN UNIVERSITY OF APPLIED SCIENCES



29.07.2016

IMPROVEMENT OF STUDENTS' UNDERSTANDING OF ALGEBRA OF SETS AND VENN-DIAGRAMS

Preface:

The basics of set theory consists in sets, elements, lists, setbuilder notation, subsets, equal sets, the empty set, union, intersection, difference, symmetric difference and Cartesian product and power sets.

Sets are one of the most fundamental concepts in mathematics but we can't calculate with set operations and set relations on any calculators, e.g. on the ClassPad. On the other hand we can write in the text mode with special symbols of the set theory in the ClassPad, e.g. \in , \notin , \cup , \cap , \setminus , \subset , \subseteq , \neq ,



1. Introduction:

Some students of informatics tried to introduce the set theory in the operating system of the calculator.

They followed several ways of solution:

- 1. Create a so called **AddIn for ClassPad330** to calculate with sets of real numbers or finite sets of words and
- 2. Create a **Basic-program for ClassPad400** to calculate with finite sets of numbers or words.
- 3. For the visualizing we get **Venn-diagrams** for a basic set Ω and up to four subsets A, B, C, D of Ω .
- 4. An important application consists in the **basics of probability theory** if the sets are random events.

Examples of Sets:

In the mathematics these days essentially everything is a set.

Some **knowledge of the set theory** is a necessary part of the background everyone needs for the further study of math.

We want to review here elementary-school set theory and the algebra of sets. Finally we will use the calculator to compute and draw Venn-diagrams.

A set is a collection of things (called its members or elements), e.g. the set of the **prime numbers** less 10: **A={2,3,5,7}** or the **set B of all real solutions of the polynomial equation** $x^{4}-17x^{3}+101x^{2}-247x+210=0$, i.e. B=A. B and A were defined in different ways.

Let be $\emptyset = \{x \mid x \neq x\}$ the **empty set**. We can form the set $\{\emptyset\}$ and $\{\{\emptyset\}\}\$ and finally $\{\emptyset, \{\emptyset\}, \{\{\emptyset\}\}\}\$, a three element set.



Two other familiar operations on sets are the **union** and **intersection**.

For example $\{x,y\} \cup \{z\} = \{x,y,z\}$ or $\{2,3,5,7\} \cap \{1,2,3,4\} = \{2,3\}$.

Any set A will have one or more subsets.

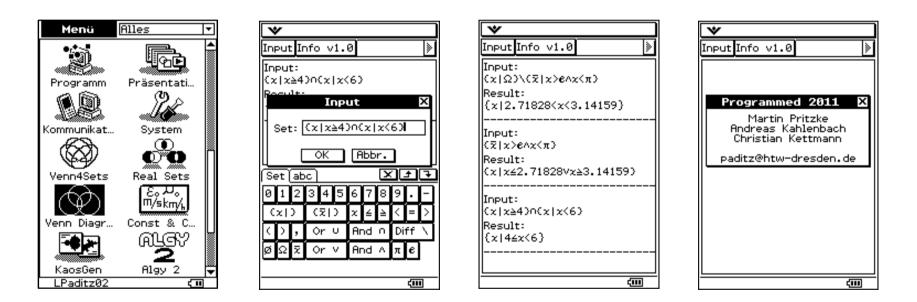
In fact if A has n elements then A has 2ⁿ subsets.

We can gather all of the subsets of A into one collection called the **power set** of A.

For example the **power set of {0,1}** is $\{\emptyset, \{0\}, \{1\}, \{0,1\}\}$ and the **power set of** \emptyset is $\{\emptyset\}$ and the **power set of {0}** is $\{\emptyset, \{\emptyset\}\}$.

2. The AddIn "REAL SETS" for ClassPad330:

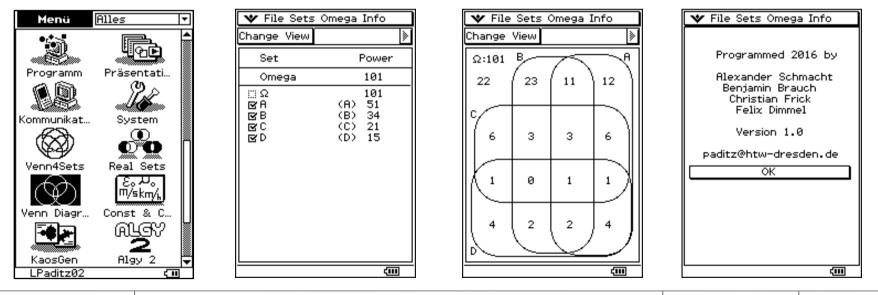
The students wrote a program in C⁺⁺ and used then the CASIO-SDK (software development kid) to compile the source program into a ClassPad AddIn.





Other students wrote a program in C⁺⁺ and used then the CASIO-SDK (software development kid) to compile the source program into a ClassPad AddIn.

Let be $\Omega = \{0, 1, 2, 3, \dots, 99, 100\},\$ A= $\{0, 2, 4, 6, \dots, 98, 100\},\$ B= $\{0, 3, 6, 9, \dots, 96, 99\},\$ C= $\{0, 5, 10, 15, \dots, 95, 100\},\$ D= $\{0, 7, 14, 21, \dots, 91, 98\}$



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29.07.2016

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4. THE PROGRAM "STROVENN" FOR CP400

The program **StrOVenn** works with sets, which are **Str**ingvariables. The **O**utput is a **Venn**-diagram. Therefore the program is named **StrOVenn**. The syntax of the input is

StrOVenn(Ω,A,B,C,D,4,2,1) or

StrOVenn(Ω,A,B,C,dummy,3,2,1) or

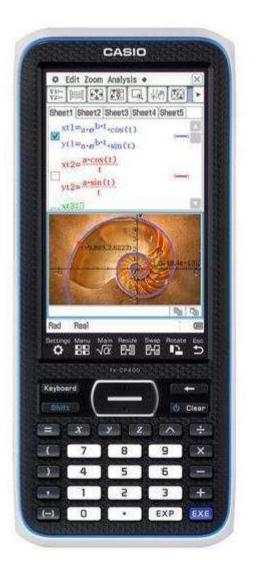
StrOVenn(Ω,A,B,dummy,dummy,2,2,1).

The last parameter 1 describes the type of data: numeric or alpha-numeric sets. Later the parameter 0 in the last position should be for the single type: numeric sets. Finally the fixed parameter 2 stands for a color Venn-diagram (ClassPad400) or 1 for a black/white diagram (ClassPad330).

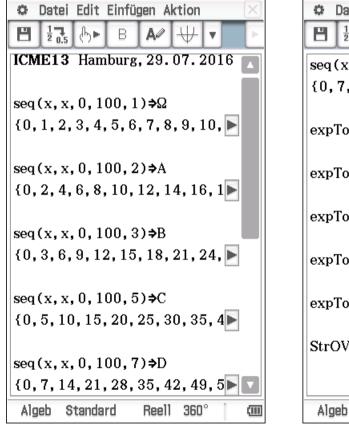


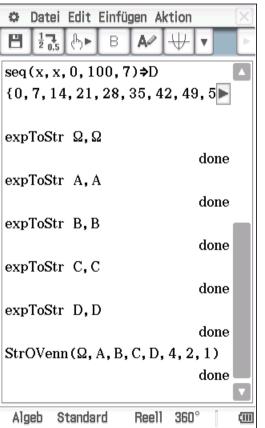
The tool – ClassPad 400

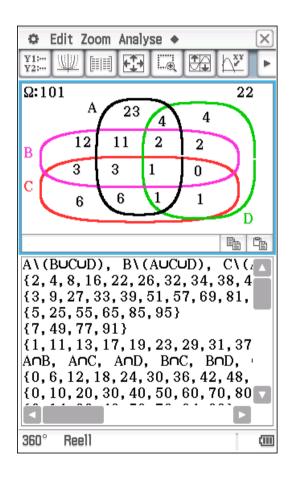
Again let be $\Omega = \{0, 1, 2, 3, 4, 5, \dots, 99, 100\}^{"}$ $A = \{0, 2, 4, 6, 8, 10, \dots, 98, 100\}^{"}$ $B = \{0, 3, 6, 9, 12, 14, \dots, 96, 99\}^{"}$ $C = \{0, 5, 10, 15, 20, \dots, 95, 100\}^{"}$ $D = \{0, 7, 14, 21, 28, \dots, 91, 98\}^{"}$



With **StrOVenn(\Omega, A, B, C, D, 4, 2, 1)** we get the results:







With the PC-ClassPad Manager we get the full screen:

🜣 Edit	×
$(BUCUD), B(AUCUD), C(AUBUD), D(AUBUC), \Omega(AUBUCUD)$	
2, 4, 8, 16, 22, 26, 32, 34, 38, 44, 46, 52, 58, 62, 64, 68, 74, 76, 82, 86, 88, 92, 94}	
3, 9, 27, 33, 39, 51, 57, 69, 81, 87, 93, 99}	
5, 25, 55, 65, 85, 95}	
7, 49, 77, 91}	
1, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97	
nB, AnC, AnD, BnC, BnD, CnD, AnBnC, AnBnD, AnCnD, BnCnD, AnBnCnD	
0, 6, 12, 18, 24, 30, 36, 42, 48, 54, 60, 66, 72, 78, 84, 90, 96}	
0, 10, 20, 30, 40, 50, 60, 70, 80, 90, 100}	
0, 14, 28, 42, 56, 70, 84, 98}	
0, 15, 30, 45, 60, 75, 90}	
0, 21, 42, 63, 84}	
0, 35, 70}	
0, 30, 60, 90}	
0, 42, 84}	
0,70}	
0}	
0}	
AnB)\(CuD), (AnC)\(BuD), (AnD)\(BuC), (BnC)\(AuD), (BnD)\(AuC), (Cr	$D) \setminus (A \cup B)$
6, 12, 18, 24, 36, 48, 54, 66, 72, 78, 96}	2, 101-2,
10, 20, 40, 50, 80, 100}	
14, 28, 56, 98}	
15. 45. 75}	
21,63}	
35}	
AnBnC)\D.(AnBnD)\C.(AnCnD)\B.(BnCnD)\A	
30,60,90}	
42,84}	
70}	
	(111

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A student discovered all prime numbers between 0 and 100 in the set

where 1 is no prime number, but 2 (not in this set).

Probability theory: Let $P(\omega)=1/n$, for all $\omega \in \Omega$ and $n=|\Omega|=101$ What is the probability $P((A \cap B) \setminus (C \cup D))$ of the difference $(A \cap B) \setminus (C \cup D)$?

What is the conditionel probability $P((A \cap B)|(C \cup D))$ with the condition $(C \cup D)$?

By the help of the Venn-diagram it is easy to get the solution.

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Wallisch, F. (2015):

mp4-video of a student:

"Testdurchlauf-vierMengen"

http://www.informatik.htw-dresden.de/ ~paditz/Testdurchlauf-vierMengen.mp4



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